

Evaluation of Fiber-Reinforced Asphalt Mixtures Using Advanced Material Characterization Tests

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ABSTRACT

A mixture of polypropylene and aramid fibers was used in this study to evaluate the performance characteristics of a modified asphalt mixture. In coordination with the City of Tempe, an asphalt concrete conventional mixture was selected for paving on Evergreen Drive in Tempe, Arizona. The designated road section within the construction project utilized two asphalt mixtures as part of this study: a control mix with no fibers, and a mixture that contained one pound of fibers per ton of asphalt concrete. The laboratory experimental program included: triaxial shear strength, dynamic (complex) modulus, repeated load permanent deformation, beam fatigue, crack propagation, and indirect diametral tensile tests. The data was used to compare the performance of the fiber modified mixture to the control. The results showed that the fibers improved the mixture's performance in several unique ways against the anticipated major pavement distresses: permanent deformation, fatigue cracking, and thermal cracking.

INTRODUCTION

Fibers have been used to improve the performance of asphalt mixtures against permanent deformation and fatigue cracking (1, 2, 3). Recent development in materials characterization tests in the pavement community was the motivation for this study to re-evaluate the performance of fiber-reinforced asphalt mixtures. Of particular interest were laboratory tests that were included as part of the National Cooperative Highway Research Program (NCHRP) 9-19 Project and the Mechanistic-Empirical Pavement Design Guide (4).

Very few research studies reporting on experiments using synthetic fibers with asphalt concrete have been found in the literature. Bueno et al studied the addition of randomly distributed synthetic fibers on the mechanical response of a cold-mixed, densely graded asphalt mixture using the Marshall test, as well as static and cyclic triaxial tests (1). The results showed that the addition of fibers caused small variations in the mixture's triaxial shear strength parameters. Lee et al evaluated the influence of recycled carpet fibers on the fatigue cracking resistance of asphalt concrete using fracture energy (3). They found that the increase in fracture energy represents a potential for improving asphalt fatigue life.

In this study, a construction project to utilize fibers in conventional asphalt concrete mixture was coordinated with the City of Tempe, Arizona. An asphalt concrete mixture designated as Type C-3/4 base and surface course was selected for paving on Evergreen Drive located east of the Loop 101 and north of University Drive in Tempe, Arizona. The designated road section had two asphalt mixtures: a control mix with no fibers, and a mixture that contained one pound of fibers per ton of mix. The fibers were a blend of polypropylene and aramid. The addition of fibers was done at a batch asphalt plant in Phoenix. Figure 1 shows the road section condition before it was overlaid. Basically, no repair work was done and the 2-inch overlay was placed on a much-deteriorated section of Evergreen Drive. Only the edge of the pavement was milled off to match the final overlay grade of the curb. Test sections with and without fibers were staggered on the road to allow for direct field performance comparisons considering traffic flow and loading types (e.g., bus lanes). About 1500 lbs of each mixture were brought back to Arizona State University (ASU) laboratories. Sample preparation included compaction of 150 mm diameter gyratory specimens for triaxial testing. In addition, beam specimens were prepared and compacted according to AASHTO TP8 test protocols (5, 6). The performance of both mixtures was assessed using the advanced material characterization tests that included: triaxial shear strength, dynamic modulus, repeated load for permanent deformation characterization, flexural beam tests for fatigue, C* line integral for fracture energy and crack propagation, and indirect diametral tensile test for thermal cracking evaluation.

OBJECTIVE

The objective of this study was to evaluate the material properties of conventional (control) and fiber-reinforced asphalt mixtures using the most current laboratory tests adopted in the pavement community. The goal was to assess how the material properties for the modified fiber-reinforced mixture differs in stiffness, permanent deformation, and cracking characteristics.



FIGURE 1 (a) Pavement Section before the Fiber-Reinforced Asphalt Concrete Mixture Overlay; (b) Surface Preparation by Milling off the Edge of the Pavement.

MATERIALS

Fibers Characteristics

The fibers used in this work were a blend of synthetic fibers designed for use in Hot Mix Asphalt (HMA) applications. The blend consisted of a proprietary blend of polypropylene and aramid fibers. Figure 2 (a) shows typical fibers contained in one-lb bag (approximately 445.0 g), of the aramid and polypropylene. Table 1 shows the main physical properties of both fibers. The fibers are designed to reinforce the HMA in three-dimensions.

TABLE 1 Physical Characteristics of Used Fibers

Materials	Polypropylene	Aramid
Form	Twisted Fibrillated Fiber	Multifilament Fiber
Specific Gravity	0.91	1.45
Tensile Strength (MPa)	483	3000
Length (mm)	19.05	38.1
Color	N/A	N/A
Acid/Alkali Resistance	inert	good
Decomposition Temperature (°C)	157	>450

Mixture Characteristics

A City of Phoenix designated asphalt mixture specification (PHX C-3/4) with nominal maximum aggregate size of $\frac{3}{4}$ -in was used. The asphalt binder used in the mix was a PG 70-10. The Theoretical Maximum Specific Gravity of the control and fiber-reinforced mixtures were 2.428 and 2.458, respectively. The design asphalt cement content was 5.0% for both mixtures. The reference air voids for both control and fiber-reinforced asphalt mixtures was 7.0%. Figure 2 (b) shows a close up of a loose asphalt mixture that was spread on the table for preparation of the

Rice gravity test. Fibers were seen by the naked eye with very good distribution throughout the mix. The mixes were re-heated and re-compacted into 150 x 170 mm Gyratory specimens. Cylindrical samples were cored from each gyratory plug, and the ends were sawed to get final specimens of 100 mm in diameter and 150 mm in height for triaxial testing. In addition, beam specimens were prepared for fatigue cracking evaluation. For thermal cracking evaluation, disc specimens were prepared according to the “Test Method for Indirect Tensile Creep Testing of Asphalt Mixtures for Thermal Cracking” reported in NCHRP Report 465 (4). Similar disc specimens were prepared for the C* crack propagation test.



FIGURE 2 (a) Close up of Reinforced Fibers: Polypropylene and Aramid (b) A Close-Up of the Fiber-Reinforced Asphalt Mixture.

TEST RESULTS AND ANALYSES

Triaxial Shear Strength Tests

The triaxial shear strength test has been recognized as the standard test for determining the strength of materials for over 50 years. The results from these tests provide a fundamental basis which can be used in analyzing the stability of asphalt mixtures. This is because the stresses acting on the laboratory specimen during the test simulate the state of stresses existing in the pavement, provided certain specimen boundary and geometry conditions are met.

Three triaxial strength stress states, one unconfined and two confined, were conducted for the control and fiber-reinforced asphalt concrete mixtures. Tests were carried out on cylindrical specimens, 4 inches (100 mm) in diameter and 6 inches (150 mm) in height. The tests were conducted at 130 °F (54.4 °C). The confining pressures used were 20 psi (138 kPa) and 40 psi (276 kPa). The specimens were loaded axially to failure at a strain rate of 1.27 mm/mm/min.

Figure 3 (a) shows a plot of the Mohr-Coulomb failure envelope represented by the cohesion “c” and angle of internal friction “ ϕ ” for the tested mixtures (2 samples for each confinement). The parameters “c” and “ ϕ ” are the strength indicators of the mixtures. The larger the “c” value, the larger the mix resistance to shearing stresses. In addition, the larger the “ ϕ ” value, the larger the capacity of the asphalt mixture to develop strength from the applied loads, and hence, the smaller the potential for permanent deformation. The “c” value of the fiber-reinforced mix was higher (34.3 psi) than that of the control mixture (27.4 psi). The effect of

fibers on the “ ϕ ” value was less, 48° for the fiber-reinforced mix versus 47° for the control mixture. Classically, the “ ϕ ” value is an aggregate property and therefore no significant variation was expected since both mixtures had the same aggregate gradations.

Figure 3 (b) presents a comparison of the tests conducted for both mixtures at 20 psi (138 kPa) confinement level. The plots represent before and after peak stress development during the test. For the fiber-reinforced mixture, it is observed that the peak stress developed and the time of its occurrence are higher when compared to those of the control mixture, a behavior that was attributed to the influence of the fibers in the mix. The fibers provide this additional reinforcement to the asphalt mix in resisting permanent deformation and retard the occurrence of shear failure. In addition, cumulative areas under the curve for the tested mixtures were calculated; the value of these areas can be interpreted as indicators of the mixes’ residual energy in resisting crack propagation post peak stress. In all tests, the fiber-reinforced mixture showed higher residual energy than the control mixture.

Repeated Load Permanent Deformation Test

The repeated load or Flow Number (FN) test is a dynamic creep test used to determine the permanent deformation characteristics of paving materials. It has been thoroughly documented in the NCHRP Report 465 study (4). In this test, a repeated dynamic load is applied for several thousand repetitions, and the cumulative permanent deformation, including the beginning of the tertiary stage (defined as FN) as a function of the number of loading cycles over the test period is recorded. Tests are carried out on cylindrical specimens, 4 inches (100 mm) in diameter and 6 inches (150 mm) in height. A haversine pulse load of 0.1 sec and 0.9 sec dwell (rest time) is applied.

Table 2 presents a master summary of the FN test results conducted at 130°F . The FN values of fiber-reinforced mixtures were found to be 15 times higher than the control mixture. The average permanent axial strain values were 0.78% and 0.51% for the control and fiber-reinforced mixtures, respectively. Two characteristics were observed for the fiber-reinforced mixture in these tests: an extended endurance period in the secondary stage, and the gradual (less) accumulation of permanent strain beyond tertiary flow. Figure 4 presents the values of strain slope for both mixtures during the tertiary stage. It can be observed that the control mix has higher strain slopes compared to the fiber-reinforced mixture. Lower values of strain slope during the tertiary stage means more energy is stored in the sample, and that the mix has higher potential to resist shear failure and further development of permanent deformation.

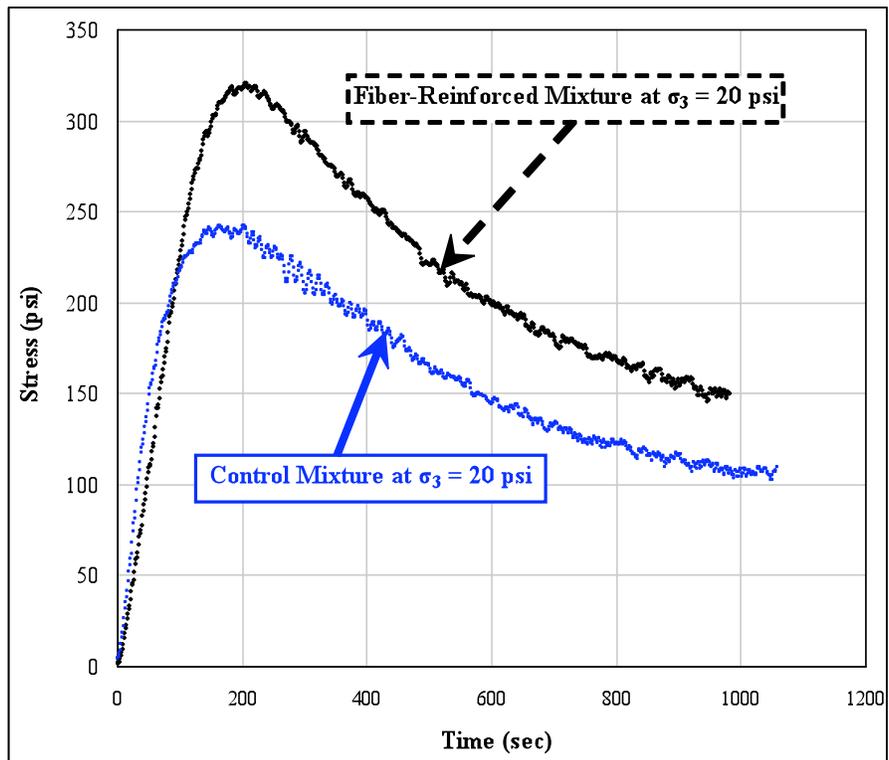
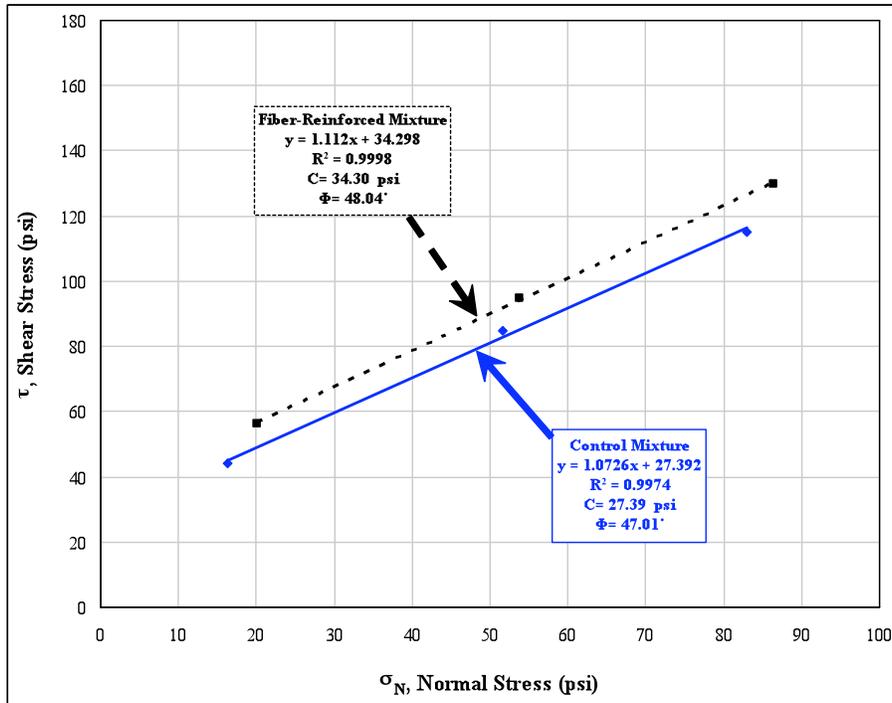


FIGURE 3 Comparison of (a) Mohr-Coulomb Envelopes (b) Stress-Time Plots at 20 psi Confinement Level.

TABLE 2 Master Summary of the Repeated Load Permanent Deformation Test Results

Mix Type	σ_d (psi)	Flow Number (Cycles)	Axial Permanent Strain ϵ_p [%] at Failure
Control	15	436	0.84
	15	241	0.56
	15	166	0.95
	Average	281	0.78
	Standard Deviation	139	0.20
	% Coefficient of Variation	49.6	25.8
Fiber-Reinforced	15	3336	0.47
	15	3466	0.60
	15	5916	0.46
	Average	4,239	0.51
	Standard Deviation	1,453	0.08
	% Coefficient of Variation	34	15.3

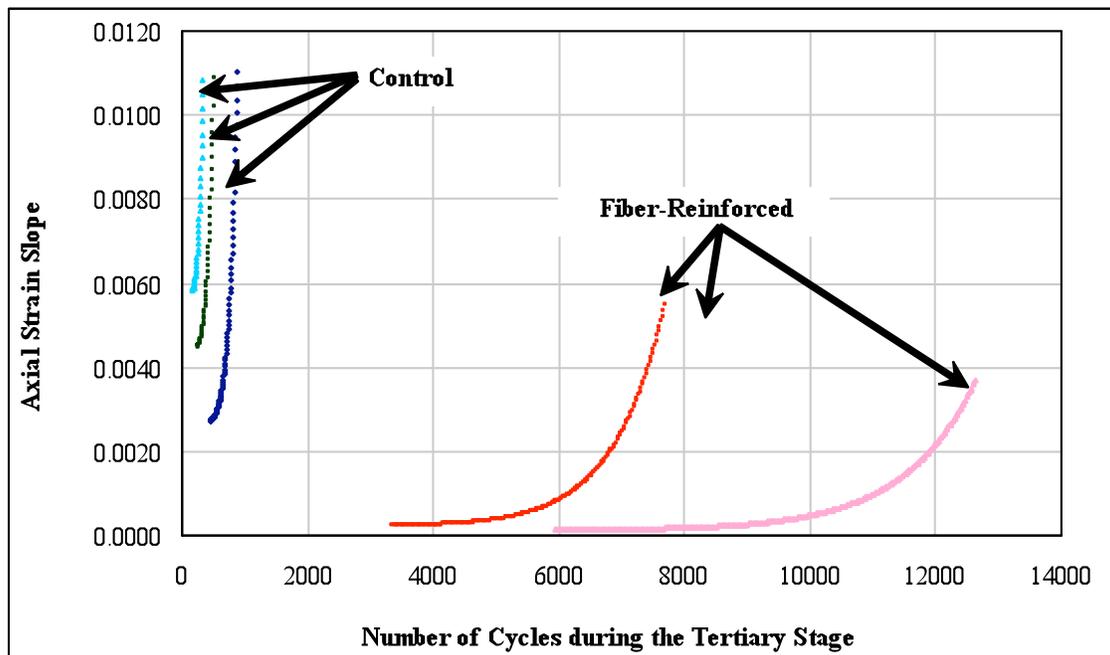


FIGURE 4 Axial Strain Slope during the Tertiary Stage for Control and Fiber-Reinforced Mixtures.

E* Dynamic Modulus Test

The stress-to-strain relationship for an asphalt mixture under a continuous sinusoidal loading is defined by its complex dynamic modulus (E^*). In the Mechanistic Empirical Pavement Design Guide (MEPDG), the E^* Dynamic Modulus of an asphalt mixture is determined per AASHTO TP 62-03. For each mix, three specimens, 4 inches (100 mm) in diameter and 6 inches (150 mm) in height, were tested at 14, 40, 70, 100, and 130 °F and 25, 10, 5, 1, 0.5, and 0.1 Hz loading frequencies. The E^* tests were done using a controlled sinusoidal stress that produced strains smaller than 150 micro-strain. A master curve was constructed at a reference temperature of 70 °F (21 °C).

Figure 5 (a) shows the average E^* master curves for both the control and fiber-reinforced asphalt concrete mixtures. The figure can be used for general comparison of the mixtures, but specific comparison of temperature-frequency combination values need to be evaluated separately. That is, one cannot compare direct values on the vertical axis for a specific log reduced time values. As shown in the figure, the fiber-reinforced mixture had higher moduli values than the control mixture at all test temperatures and frequencies. The difference is less at the lowest temperature due to dominant effect of the binder. At higher temperatures, the binder becomes softer and the aggregates dominate the elastic behavior of the asphalt mixtures, and the reinforcement effect of the fibers can enhance the modulus values at higher temperatures. In addition, the aramid fibers have a unique negative thermal coefficient value, in that they contract at higher temperatures and therefore play a positive role in resisting deformation. Figure 5 (b) shows direct comparisons for selected values of test temperatures, 40, 100, and 130 °F (4.4, 37.8 and 54.4 °C) and loading frequency of 10 Hz. It is observed that the modulus values for the fiber-reinforced mixture are higher than the control mixture. Especially at high temperature conditions, the potential rutting field performance of the fiber-reinforced mix would be better than that of the control mixture.

Fatigue Cracking Test

Load-associated fatigue cracking is one of the major distress types occurring in flexible pavement systems. The action of repeated loading, caused by traffic induced tensile and shear stresses in the bound layers, will eventually lead to a loss in the structural integrity of a stabilized layer material. Fatigue will induce cracks at points where critical tensile strains and stresses occur. The most common model form used to predict the number of load repetitions to fatigue cracking is a function of the tensile strain and mix stiffness (modulus) as follows (6):

$$N_f = K_1 \left(\frac{1}{\epsilon_t} \right)^{k_2} \left(\frac{1}{E} \right)^{k_3} = K_1 (\epsilon_t)^{-k_2} (E)^{-k_3}$$

Where:

N_f = number of repetitions to fatigue cracking

ϵ_t = tensile strain at the critical location

E = stiffness of the material

K_1, K_2, K_3 = laboratory calibration parameters

In this study, beam specimens were prepared for the three point bending test using the reheated mixtures obtained during construction. After compaction to the required density (7% air voids), beams were saw cut to the required dimensions of 2.5 inches (63.5 mm) wide, 2.0 inches

(50.8 mm) high, and 15 inches (381 mm) long. A full testing factorial was used for each mixture: constant strain, 6 to 8 levels, and one replicate for each test temperature. Three temperature levels, 40, 70, 100 °F, (4.4, 21, and 38.8 °C) were used. Initial flexural stiffness was measured at the 50th load cycle. Fatigue life or failure under control strain was defined as the number of cycles corresponding to a 50% reduction in the initial stiffness as required by AASHTO TP8 and SHRP M-009.

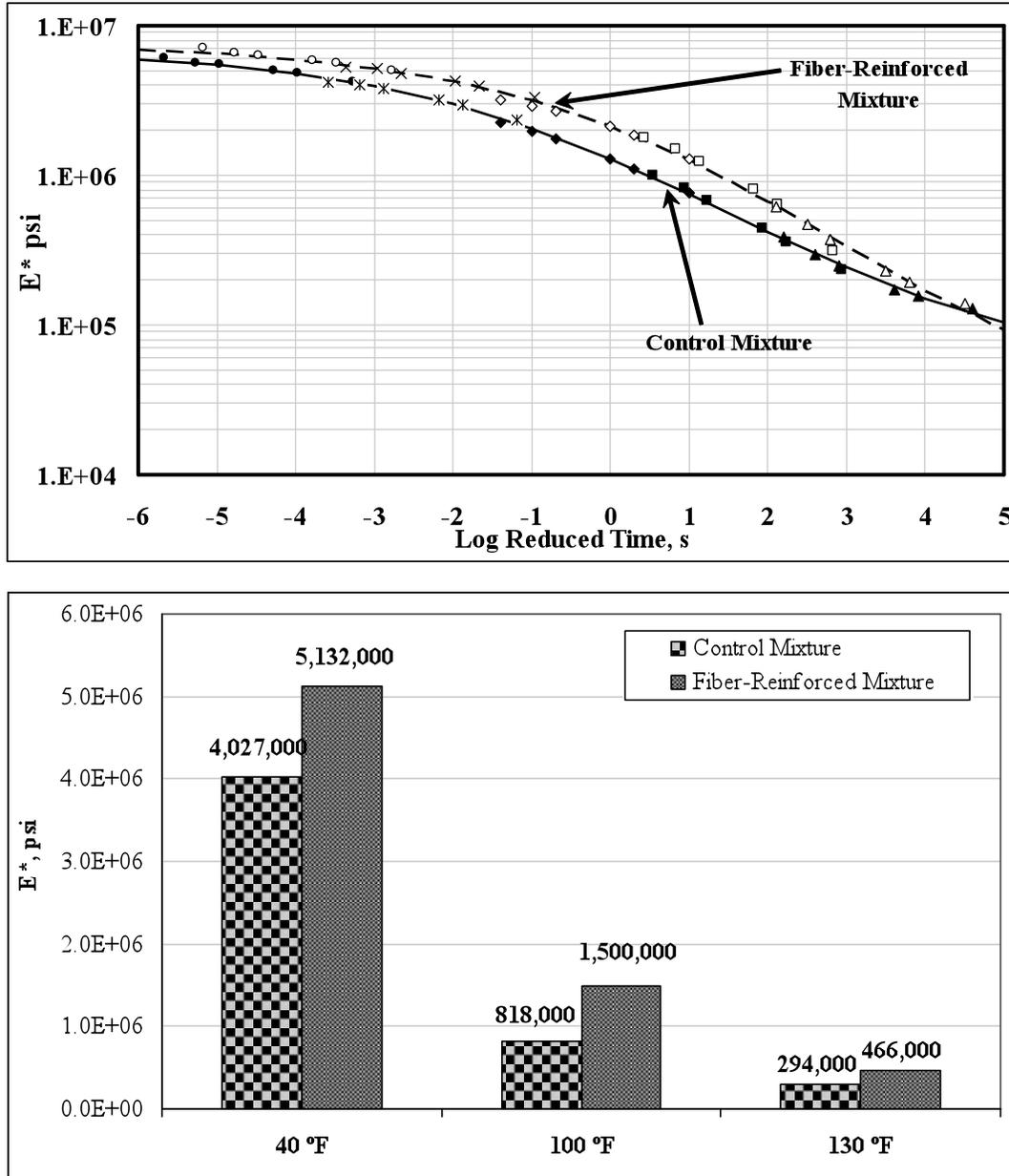


FIGURE 5 (a) Unconfined Dynamic Modulus Master Curves; (b) Comparison of Measured Dynamic Modulus Values at 10 Hz.

Fatigue relationships for both mixtures were developed. The regression equations for each temperature ($N_f = K_1 \cdot \epsilon^{K_2}$) were also computed along with the coefficient of determination

(R^2) for each relationship. Figure 6 shows a comparison of fatigue relationships for the control and fiber-reinforced asphalt concrete mixtures at 70 °F. It is observed that the fatigue life is higher for the control mixture at high strain values while the fiber-reinforced mixture has higher fatigue life at lower strain values.

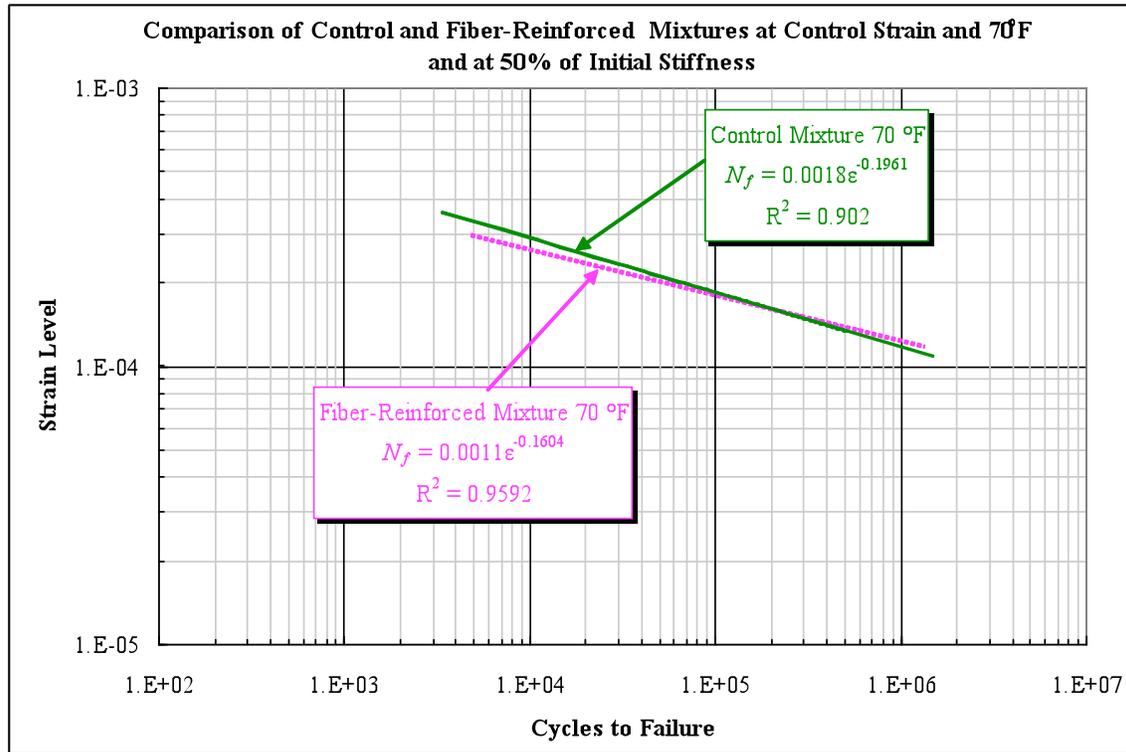


FIGURE 6 Comparison of Fatigue Relationships for both Mixtures at 70 °F.

Table 3 summarizes the K_1 , K_2 , and K_3 Coefficients of the generalized fatigue model for both mixtures (at 50% reduction of the initial stiffness). The initial stiffness was measured at $N = 50$ cycles. These generalized fatigue relationships show excellent measures of accuracy for both mixtures.

TABLE 3 Summary of the Regression Coefficients for the Generalized Fatigue Equation

Mixture Type	50% of Initial Stiffness, E_o @ $N=50$ Cycles			
	K_1	K_2	K_3	R^2
Control	2.3496	2.3601	1.3853	0.914
Fiber-Reinforced	6.48E-22	7.8357	1.0839	0.988

$$* N_f = K_1 * (1/\epsilon_t)^{K_2} * (1/E_o)^{K_3}$$

An example comparing the fatigue life for both mixtures was predicted using the regression coefficients K_1 , K_2 , and K_3 at 70 °F and two different strain levels. The results are

shown in Figure 7. At 150 micro-strains level, the fiber-reinforced mixture shows approximately 2 times higher fatigue life compared to the control mixture; while at 200 micro-strains level, the control mixture shows approximately 3 times higher fatigue life compared to the fiber-reinforced mixture. The shift in predicted fatigue life suggests that the fiber-reinforced mix will perform better in roads where traffic speeds are higher. This type of fatigue testing is a disadvantage for a stiffer material like the fiber-reinforced mixture. These results may be labeled as inconclusive, and is worthy of more investigation.

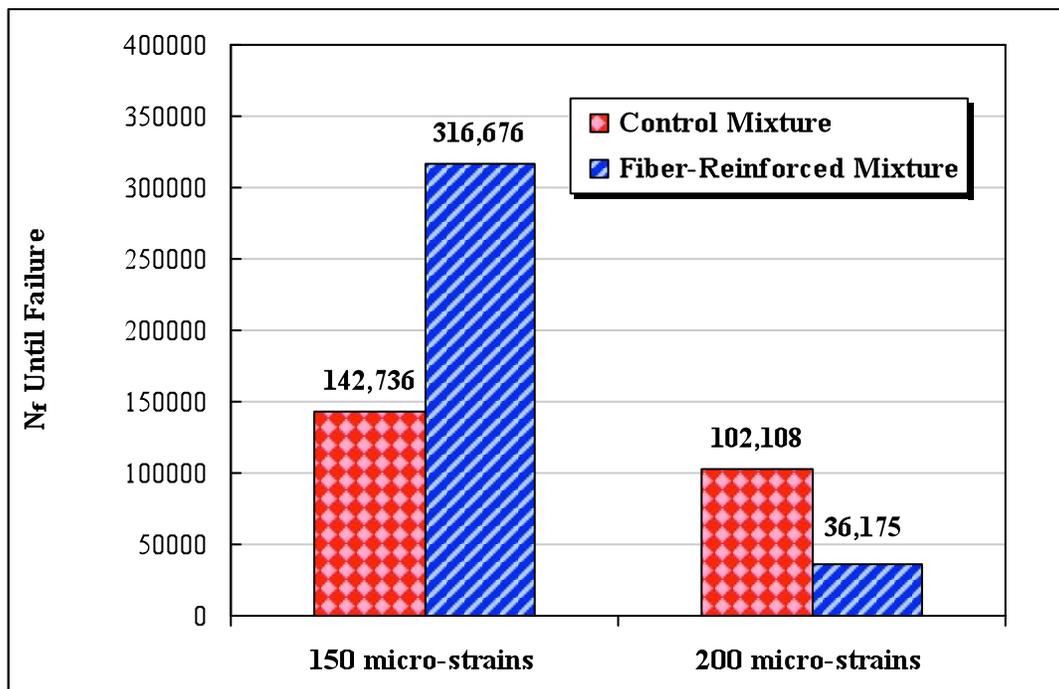


FIGURE 7 Number of Cycles to Failure Predicted for Both Mixtures at 150 and 200 micro-strains and at 70 °F.

Thermal Cracking Test

Standard test method for determining the creep compliance and strength of HMA using the indirect tensile test device per AASHTO TP9-02 was utilized to evaluate low temperature thermal cracking performance of the control and the fiber-reinforced asphalt concrete mixtures (7, 8). Figure 8 presents the tensile strength test results for both mixtures. The fiber-reinforced asphalt mixture has 1.5 times higher strength than the control mixture. Higher thermal cracking would be expected for mixtures with lower tensile strength values (4). In essence, the fibers in the mix are believed to play a vital role in resisting thermal cracking in the HMA mixture.

The consideration of the total fracture energy is another useful comparison from this test. The results are shown in Figure 9. The fracture energy increased with increasing temperature for both the mixtures. At all test temperatures, the fiber-reinforced asphalt mixture had consistently higher fracture energy than the control mix. Generally, lower thermal cracking should be expected as the fracture energy is increased (4).

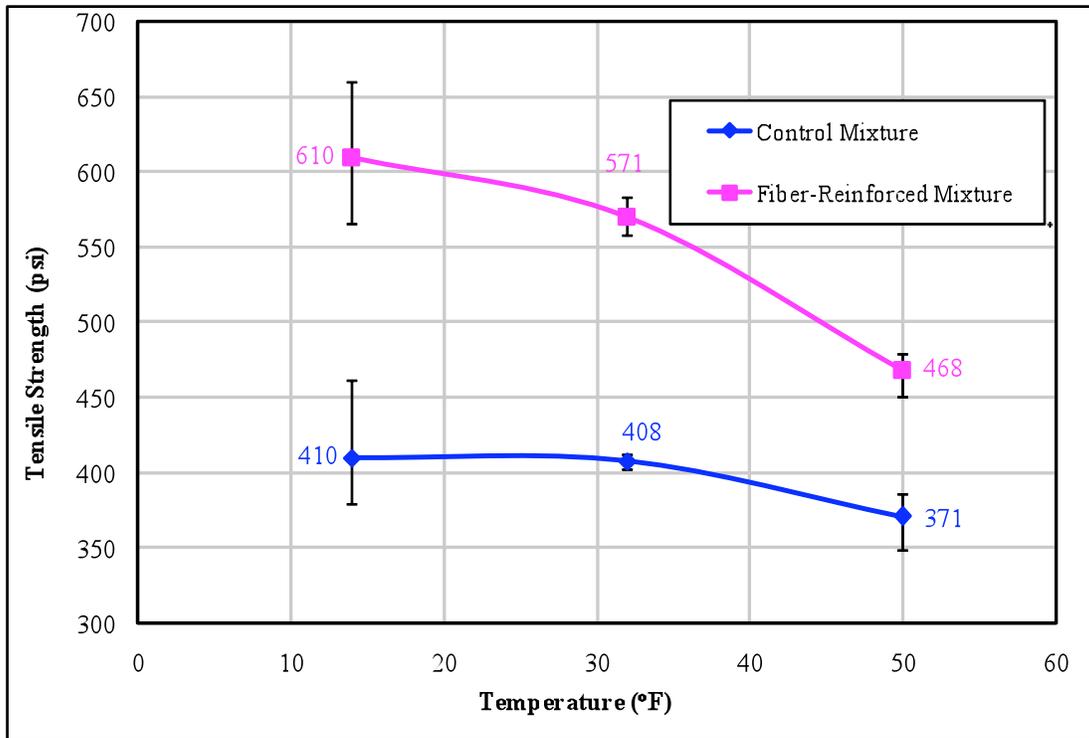


FIGURE 8 Comparison of the Tensile Strength Results.

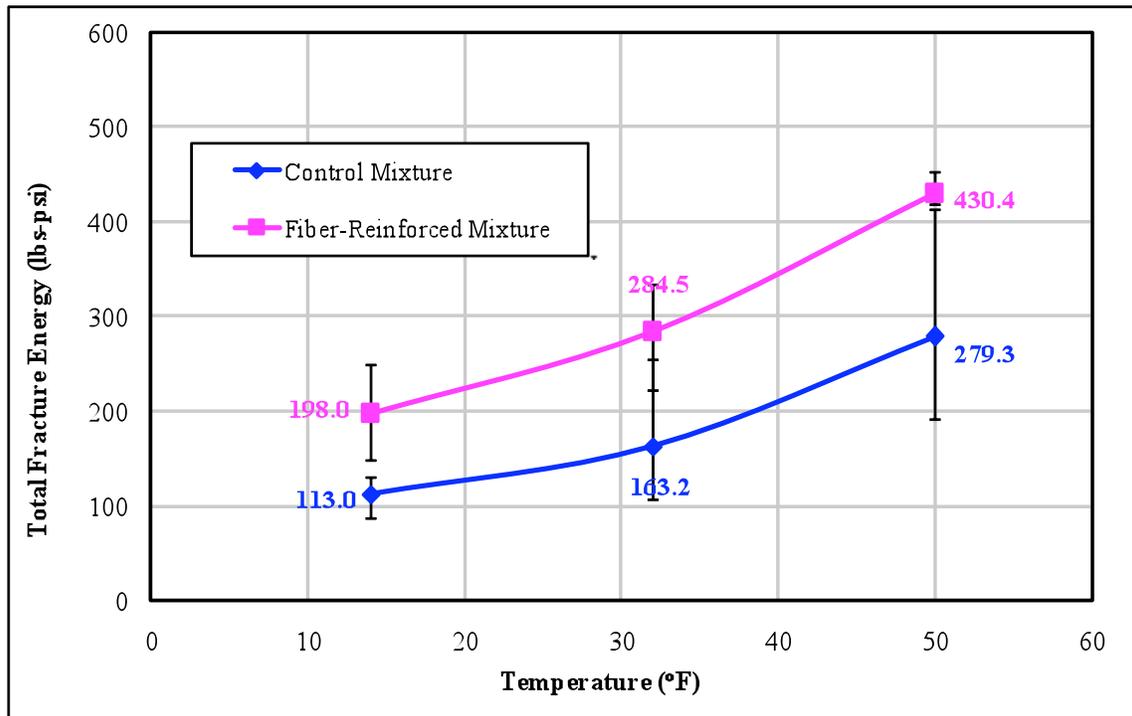


FIGURE 9 Comparison of the Total Fracture Energy Results.

Crack Propagation - C* Line Integral Test

Fracture mechanics provides the underlying principles which govern initiation and propagation of cracks in materials. Sharp internal or surface notches which exist in various materials intensify local stress distribution. If the energy stored at the vicinity of the notch is equal to the energy required for the formation of new surfaces, then crack growth can take place. Material at the vicinity of the crack relaxes, the strain energy is consumed as surface energy, and the crack grows by an infinitesimal amount. If the rate of release of strain energy is equal to the fracture toughness, then the crack growth takes place under steady state conditions and the failure is unavoidable (9).

The concept of fracture mechanics was introduced to asphalt concrete by Majidzadeh (10). Abdulshafi applied the energy (C*-Line Integral) approach to predicting the pavement fatigue life using the crack initiation, crack propagation, and failure (11). Abdulshafi, O., and Abdulshafi, A. and Kaloush used notched disk specimens to apply J-integral concept to the fracture and fatigue of asphalt pavements (11, 12).

C* Parameters

The relation between the J-integral and the C* parameters is a method for measuring it experimentally. J is an energy rate and C* is an energy rate or power integral. An energy rate interpretation of J has been discussed by Rice; and Begley and Landes (13, 14). J can be interpreted as the energy difference between the two identically loaded bodies having incrementally differing crack lengths.

$$J = - \frac{dU}{da}$$

Where,

U = Potential Energy

a = Crack Length

C* can be calculated in a similar manner using a power rate interpretation. Using this approach C* is the power difference between two identically loaded buddies having incrementally differing crack lengths.

$$C^* = - \frac{\partial U^*}{\partial a}$$

Where U* is the power or energy rate defined for a load p and displacement u by:

$$U^* = \int_0^u p du$$

Method for C* Determination

Disc samples were prepared from gyratory plugs similar to the IDT specimen preparation process. For each disc, a right-angle wedge was cut into the specimen to accommodate the loading device as shown in Figure 10. Tests were conducted at 21° C.

The load applied at a constant displacement rate and the crack length over time were measured for each test specimen. The displacement rates used were 0.005, 0.01, 0.015, 0.02, and 0.025 in/min for both the control and fiber-reinforced mixtures. The data was used to determine load as a function of displacement rate for various crack lengths. The power of energy rate input, U*, was measured as the area under the load displacement rate curve. The energy rate, U*, was

then plotted versus crack length for different displacement rates and the slopes of these curves constituted the C*-integral. The C*-integral was plotted as a function of the displacement rate. Finally, the C* integral data were plotted as a function of the crack growth rate as shown in Figure 11. In this figure, it is observed that the fiber-reinforced mixture has much higher C*-integral and slope values compared to the control mixture. This is an indication that the fiber-reinforced mixture has much higher resistance to crack propagation. A unique observation of the fiber-reinforced mix specimens after the test was that the samples never split and they were difficult to split them apart by hand; whereas most of the control mixture samples split at the end of the test.

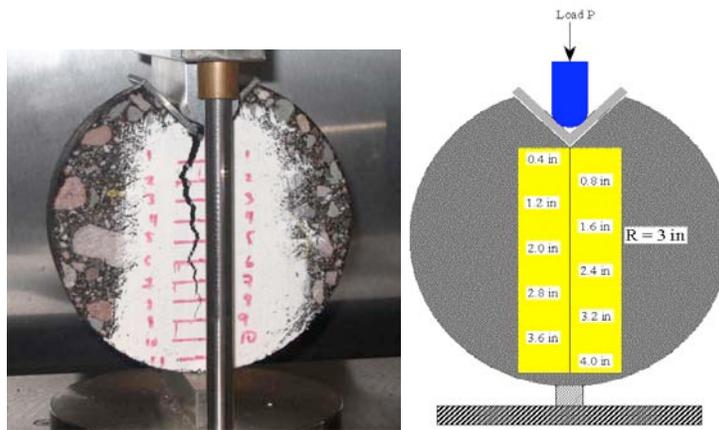


FIGURE 10 Typical C* Test Setup.

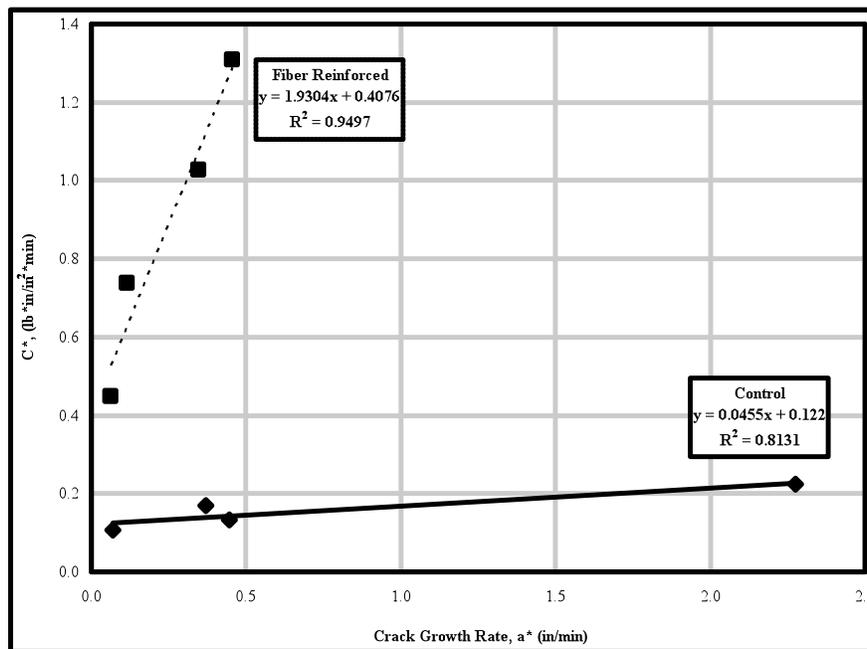


FIGURE 11 C* Line Integral versus Crack Growth Rate.

CONCLUSIONS

A mixture of polypropylene and aramid fibers was used in a field and laboratory study to evaluate the performance characteristics of the modified asphalt mixture. The laboratory experimental program on the field mixes included: triaxial shear strength, dynamic (complex) modulus, repeated load permanent deformation, beam fatigue, crack propagation, and indirect diametral tensile tests. The data was used to compare the performance of the fiber modified mixture to the control. The results showed that the fibers improved the mixture's performance in several unique ways as summarized below:

- The fiber-reinforced asphalt mixture showed better resistance to shear deformation as shown by the triaxial shear strength test results. Notably, post peak failure for the fiber-reinforced asphalt mixture showed higher residual energy and gradual drop in strength, an effect that was attributed to the influence of the fibers in the mix.
- Permanent deformation tests for the fiber-reinforced mixture showed lower permanent strain accumulation compared to the control mix. The flow number results, or the beginning of tertiary stage, were 15 times higher than the control mixture. Two characteristics were observed for the fiber-reinforced mixture in these tests: an extended endurance period in the secondary stage of the permanent deformation curve, and the gradual (less) accumulation of permanent strain beyond tertiary flow. Both of these characteristics were attributed to the presence and mobilization of the fibers distributed in the mix.
- The measured Dynamic Modulus E^* values were higher for the fiber-reinforced mix. The difference between the two mixtures was less at the lowest temperature (20% increase), due to dominant effect of the binder and less contribution of the role of fibers. The largest difference was observed at 100°F (80% higher), where the reinforcement effect of the fibers is observed to be the highest. At 130°F, the increase in modulus was also substantial at about 50%.
- The fatigue cracking test was different in that, unlike the other tests, the strain level was held constant. The fatigue life was higher for the control mixture at high strain values while the fiber-reinforced mixture had higher fatigue life at lower strain values. The shift in predicted fatigue life suggests that the fiber-reinforced mix will perform better in roads where traffic speeds are higher. However, it was concluded that the fatigue cracking results are inconclusive and need further evaluation.
- The tensile strength and fracture energy measured from the IDT test showed that at all test temperatures, the fiber-reinforced mix exhibited the highest values; an increase of 25 to 50% for the tensile strength, and 50 to 75% for the fracture energy. Generally, lower thermal cracking should be expected as the tensile strength and fracture energy are increased.
- Relationships between crack growth rates and C^* line integral values showed that the fiber-reinforced mix had about 40 times higher resistance to crack propagation than the control mix.
- A field condition survey after approximately one year (with two summer periods included) revealed that there are a couple of low severity cracks, 1 to 2 feet long, in the control section. No cracks were observed in the fiber-reinforced pavement sections.

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